Research Article

Au_{26-35} : A Special Geometrical Structure of Au_{33} (D_2) Cluster with Highly Occupied - 14 Pairs of Double-State Degeneracy

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Abstract

In this article, an interesting phenomenon has described the geometries and vibrational frequency of the stable Au_N clusters with N = 26 to 35. We have found nine out of ten clusters are having the very same C_1 symmetry, except the cluster N = 33 (D_2). The finite-differentiation method has been implemented within the density-functional tight-binding (DFTB) approach. The effects of the range of interatomic forces were calculated and the desired set of system eigenfrequencies (3N-6) are obtained by diagonalization of the symmetric positive semidefinite Hessian matrix. Mainly, we have observed the vibrational spectra and the range comes in between 2.04 and 347.32 cm⁻¹ at ground state, $\Delta E = 0$. Most significantly, all the clusters have revealed double-state degeneracy. The vibrational spectrum is strongly dependent upon the size, shape, and structure, at the same time, the stretching and the bending mode of the atoms with respect to the bond length plays a major role. We have compared some of our results, which have an excellent agreement, with the less availability of the experimental and the theoretical predictions.

Introduction

In the past decades, gold clusters have attracted the great interest of both experimental and theoretical researchers due to their fundamental importance and tremendous potential applications in catalysis, biology, and nanoscale devices [1-12].

In general, noble-metal (Cu, Ag, and Au) clusters have attracted much attention in scientific and technological fields because of their thermodynamic, electronic, optical, and catalytic properties in nano-materials [13-15]. Especially, gold is a soft metal and is usually alloyed to give it more strength as well as a good conductor of heat and electricity, and is unaffected by air and most reagents, those are the main reasons to choose among the other metal clusters. Its physical and chemical properties appear to be entirely changing as the size of metal continuously decreases into the nanoscale because of the quantum size effect, surface effect, small size effect, and macroscopic quantum tunneling (MQT) effect [16-17].

Nanotechnology is a relatively new branch of science that has found a wide range of applications that range from energy production to industrial production processes to biomedical applications [18]. One of the key applications is in biology and

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Keywords: Gold atomic clusters; Density-Functional Tight-Binding (DFTB) approach; Finite-difference Method; Force Constants (FCs) and Vibrational spectrum





biomedical research. Nanoparticles (NPs) can be engineered to possess unique compositions and functionalities, which can provide novel tools and techniques that, have not previously existed in biomedical research. For example, NPs can be used to image biological processes on the cellular level. They can also be utilized to detect analytes at the attomolar range [19].

Nanotechnology has become a trending area in science and has made great advances with the development of functional, engineered nanoparticles. Various metal nanoparticles have been widely exploited for a wide range of medical applications. Among them, gold nanoparticles (AuNPs) are widely reported to guide an impressive resurgence and are highly remarkable. AuNPs, with their multiple, unique functional properties, and ease of synthesis, has attracted extensive attention. Their intrinsic features (optics, electronics, and physicochemical characteristics) can be altered by changing the characterization of the nanoparticles, such as shape, size, and aspect ratio. They can be applied to a wide range of medical applications, including drug and gene delivery, photothermal therapy (PTT), photodynamic therapy (PDT) and radiation therapy (RT), diagnosis, X-ray imaging, computed tomography (CT), and other biological activities [20].

Particularly, gold nanoclusters (AuNCs) have been extensively applied as fluorescent probes for biomedical applications in imaging, detection, and therapy due to their unique chemical and physical properties [21]. Recently, reported that gold phosphine complexes show anticancer activity toward a panel of different tumor cell lines [22]. In addition, gold clusters with near-infrared II (NIR-II) fluore-scence are used to monitor high-resolution imaging of kidneys at a depth of 0.61 cm, and the quantitative measurement shows 86% of the gold clusters are cleared from the body without any acute or long-term toxicity at a dose of 100 mg kg⁻¹. Bright gold clusters can penetrate deep tissue and can be applied *in vivo* brain vessel imaging and tumor metastasis [23].

In recent years, gold compounds have gained more and more attention in the design of new metal anticancer drugs. Numerous types of research have reported that gold compounds, in addition to their widely studied cytotoxic antitumor effects, also reverse tumor immune escape and directly facilitate the functions of immune cells, leading to enhanced anticancer effects [24].

Gold clusters, which display a variety of unusual geometric structures due to their strong relativistic effects, have attra-cted much attention. Among them, Au_{26} has a high-symmetry tubular structure (D_{6d}) with a large HOMO-LUMO energy gap, but its electronic stability still remains unclear. In Liu Q, *et al.* paper, the electronic nature of the Au_{26} cluster is investigated using the density functional theory method. Depending on the super valence bond model, the tubular Au_{26} cluster with 26 valence electrons could be viewed as a super atomic molecule composed of two open cages based on spherical aromaticity, and its molecule-like electronic shell closure is achieved via a super triple bond (σ , 2π) between the two cages [25].

Gold clusters are known to form many cages like geometries such as Au_{20} , Au_{24} , and Au_{32} . The shape of these clusters varies from Tetrahedral (Au_{20}) cage to Fullerene like (Au_{32}) and tubular form (Au_{24}) [26]. The Au₂₆ cluster is one of the widely studied gold clusters in the size range of N = 21-30. It has been proposed in a more recent combined experimental and theoretical study that the neutral Au_{26} cluster is fluxional. The fluxionality of a cluster is relevant to its catalytic applications [27]. The structural evolution of negatively charged gold clusters (Au_n) in the medium size range for n = 27-35 has been investigated using photoelectron spectroscopy (PES) and theoretical calculations by the research group of Nan Shao, [27]. The cage-like gold clusters would be of both fundamental and practical interest because of their high surface area (all the atoms are on the cluster surface) and hollow cavity to accommodate other atoms or molecules [28].

A surprising stability of the tube-like Au_n (n = 26-28) has been shown using the scalar relativistic all-electron density functional theory calculations, forming another powerful candidate for the lowest-energy Au_n competing with those previously suggested space-filled structures. Unlike the icosahedral "golden" fullerene Au_{32} , these tube-like gold clusters may be closely related to the synthesized single-wall gold nanotubes (SWGNT). The groundstate Au_{26} has a hollow tube-like structure constructed from the (6, 0) SWGNT, yielding a high-symmetry D_{6d} cage, based upon which the most stable Au_{27} and Au_{28} can be obtained by capped one and two atoms, respectively [29]. In total, gold is a multipurpose material that has been utilized for examining technological applications [30].

DFTB-based global searches have not been done for gold clusters in the range of Au_{26} to Au_{35} . Structural determination for larger gold clusters becomes increasingly more challenging, and global minimum searches are essential because of the sheer number of possible atomic arrangements. Except for Au_{32}^{-} and Au_{34}^{-} . In fact, the global minima of Au_{32}^{-} and Au_{34}^{-} are still controversial [31 - 37].

Most recently, Philipp Gruene, et al. have calculated, vibrational spectra of small neutral gold clusters containing up to 8 Au atoms which were measured in the far-infrared (46-222 cm⁻¹) via photodissociation of their complexes with krypton atoms. They have compared with calculated IR spectra for bare Au_N clusters using density functional theory that has allowed for structural assignment. For those small sizes, all clusters are found to be planar and of comparably high symmetry [38]. Therefore, with the highest possible, the vibrational properties could be able to calculate with the help of Infrared Intensity and partial Infrared Intensity [30]. Additionally, vibrational spectroscopy was utilized for analyzing the gold cluster structures and DFT calculations were used for the investigations of small complex gold clusters [39]. The theoretical studies on the electronic, optical, vibrational, and other physical and chemical properties of the gold clusters are at the forefront of cluster science [40].

Gold has been the major focus of the SCC-DFTB field due to its promising applications in the development of new nanodevices [41]. Moreover, the DFTB method has been utilized to design these gold clusters which are size-dependent and it is observed that quantum confinement effects narrowed the energy gap [30].

In this study, we focus mainly on the vibrational properties of gold atomic clusters with sizes Au_{26-35} atoms, because it plays a major role in structural stability [42 - 49]. Further assistance for the readers, specifically for the general information about global minima gold structures which have been calculated by the work of Dong and Springborg can be found in those articles [50, 51]. In very short, the structures were found through a socalled genetic algorithm (GA) in combination with Density Functional Tight-Binding (DFTB) energy calculations and the steepest descent algorithm permitting a local total energy minimization. Nevertheless, in our case, we use the numerical finite-difference method [52] along with the density-functional tight-binding (DFTB) approach [53 - 55] and finally extract the vibrational spectrum from the re-optimized structures.

The following section introduces the DFTB procedures used for our calculations. Overall, the depth and detailed information are discussed in the results and discussion section.

Theoretical and computational procedures

In the first step, the DFTB [53 - 55] is based on the density functional theory of Hohenberg and Kohn in the formulation of Kohn and Sham. In addition, the Kohn-Sham orbitals $\psi_i(\mathbf{r})$ of the system of interest are expanded in terms of atom-centered basis functions { $\varphi_m(\mathbf{r})$ },

$$\psi_i(\mathbf{r}) = \sum c_{im} \phi_m \ (\mathbf{r}), \ m = j. \tag{1}$$

While so far the variational parameters have been the real-space grid representations of the pseudo wave functions, it will now be the set of coefficients c_{im} . Index *m* describes the atom, where ϕ_m is centered and it is angular as well as radially dependent. The ϕ_m is determined by self-consistent DFT calculations on isolated atoms using large Slater-type basis sets.

In calculating the orbital energies, we need the Hamilton matrix elements and the overlap matrix elements. The above formula gives the secular equations

$$\sum_{m} c_{im} (H_{mn} - \epsilon_i S_{mn}) = 0 \tag{2}$$

Here, c_{im} 's are expansion coefficients, ϵ_{i} is for the singleparticle energies (or where ϵ_{i} are the Kohn-Sham eigenvalues of the neutral), and the matrix elements of Hamiltonian H_{mn} and the overlap matrix elements S_{mn} are defined as

$$H_{mn} = \langle \phi_m \mid \hat{H} \mid \phi_m \rangle, S_{mn} = \langle \phi_m \mid \phi_n \rangle \tag{3}$$

They depend on the atomic positions and on a well-guessed density $\rho(\mathbf{r})$. By solving the Kohn-Sham equations in an effective one-particle potential, the Hamiltonian \hat{H} is defined as

$$\hat{H}\psi_{i}\left(\boldsymbol{r}\right) = \epsilon_{i}\psi_{i}\left(\boldsymbol{r}\right), \hat{H} = \hat{T} + V_{eff}\left(\boldsymbol{r}\right)$$

$$\tag{4}$$

To calculate the Hamiltonian matrix, the effective potential V_{eff} has to be approximated. Here, \hat{T} being the kinetic-energy operator $\Sigma^{\hat{T}} = -\frac{1}{2}\nabla^2$ and $V_{eff}(\mathbf{r})$ being the effective Kohn-Sham potential, which is approximated as a simple superposition of the potentials of the neutral atoms,

$$V_{eff}(\mathbf{r}) = \sum_{j} V_{J}^{0}\left(\left|\mathbf{r} - \mathbf{R}_{j}\right|\right)$$
(5)

 V_j^0 is the Kohn-Sham potential of a neutral atom, $r_j = r - R_j$ is an atomic position, and R_j is the coordinates of the *j* atom.

Finally, the short-range interactions can be approximated by simple pair potentials, and the total energy of the compound of interest relative to that of the isolated atoms is then written as,

$$E_{tot} \approx \sum_{j} \epsilon_{i} - \sum_{j} \sum_{mj} \epsilon_{imj} + \frac{1}{2} \sum_{j \neq j'} U_{jj'} (|\mathbf{R}_{j} - \mathbf{R}_{j'}|)$$

$$\epsilon_{B} \equiv \sum_{i}^{occ} \epsilon_{i} - \sum_{j} \sum_{mj}^{occ} \epsilon_{imj}$$
(6)

Here, the majority of the binding energy (ϵ_B) is contained in the difference between the single-particle energies ϵ_i the of system of interest and the single-particle energies ϵ_{jm_j} of the isolated atoms (atom index *j*, orbital index *m_j*), $U_{jj'}(|\mathbf{R}_j - \mathbf{R}_{j'}|)$ is determined as the difference between ϵ_B and ϵ_B^{SCF} for diatomic molecules (with ϵ_B^{SCF} being the total energy from parameter-free density-functional calculations). In the present study, only the 5*d* and 6*s* electrons of the gold atoms are explicitly included, whereas the rest are treated within a frozen-core approximation [54 - 56].

Structural re-optimization process

This work is dedicated to the computational investigation of the gold clusters that vary with the number of atoms and becomes difficult for the computational investigation of gold clusters and required very precise and careful methodology with accuracy.

In our case, we have calculated the numerical first-order derivatives of the forces ($\mathbf{F}_{i\alpha}$, $\mathbf{F}_{j\beta}$) instead of the numerical second-order derivatives of the total energy (E_{tot}). In principle, there is no difference, but numerically the approach of using the forces is more accurate [52].

$$\frac{1}{M} \frac{\partial^2 E_{tot}}{\partial \mathbf{R}_{i\alpha} \partial \mathbf{R}_{j\beta}} = \frac{1}{M} \frac{1}{2ds} \left[\frac{\partial}{\partial \mathbf{R}_{i\alpha}} \left(-\mathbf{F}_{j\beta} \right) + \frac{\partial}{\partial \mathbf{R}_{j\beta}} \left(-\mathbf{F}_{i\alpha} \right) \right]$$
(7)

Here, $k = (\mathbf{F}_{ia}, \mathbf{F}_{ib})$ is a restoring force that is acting upon the atoms, ds is a differentiation step-size and M represents the atomic mass, for the homonuclear case. The complete list of these force constants (FCs) is called the Hessian H, which is a $(3N \times 3N)$ matrix. Here, *i* is the component of (x, y or z) of the force on the *j* atom, so we get 3*N*. The Hessian matrix is the matrix of second derivatives of the energy with respect to geometry which is quite sensitive to its geometry. Energy second derivatives are evaluated numerically. The mass-weighted Hessian matrix is obtained by numerical differentiation of the analytical first derivatives, calculated at geometries obtained by incrementing, in turn, each of the 3N nuclear coordinates by a small amount of ds with respect to the equilibrium geometry. The introduction of the Hessian matrix and its diagonalization ultimately leads to the eigenfrequencies of the system and its eigenvectors, describing the harmonic motion of the cluster atoms. In order to obtain the matrix elements H_{ii} of the Hessian matrix which is needed if one wishes to investigate the cluster's thermodynamic properties and one should obtain the derivatives of potential energy surface (PES) [57].

Results and discussions

The optimized structure of the clusters Au₂₆₋₃₅

We present the vibrational spectrum analysis of the reoptimized Au_{26-35} clusters, interestingly, all of them are having the very same point group symmetry C_1 , except Au_{33} (D_2), at ground state, $\Delta E = 0$. Initially, the structures were found through a so-called genetic algorithm (GA) in combination with Density Functional Tight-Binding (DFTB) energy calculations and the steepest descent algorithm permitting a local total energy minimization [58, 59]. To sum up, we have accurately predicted the vibrational frequency of the clusters, and they are very strongly dependent on the size, structure, and shape of the clusters [60], as well as, mainly influenced by the stretching and the bending mode vibrations of the atoms that are due to changes on the bond length fluctuations for a small step-size $ds = \pm 0.01$ a.u. on the equilibrium coordinates [61]. Importantly, these spectra are different for the different atomic configurations.

In brief, this study represents the first such one where also electronic degrees of freedom explicitly are included, which indeed turns out to be important. When including orbital interactions, not only packing but also directional interactions determine the optimal structure and, therefore, in most cases, our optimized structures do not have a very high symmetry, *i.e.*, the occurrence of magic numbers becomes much less pronounced. In this respect, again, we would like to bring your attention to, an atom of gold that seems to be special. For other metals, packing effects are often dominating, whereas, for covalently bonded elements, the effects due to directional bonds are dominating. We suggest that for gold there is a competition between the two leading to the lowsymmetry, although quite compact structures of the Au_n (n = 2-58) clusters [58, 59]. By comparing with the results of jellium calculations, it was demonstrated that for gold clusters, electronic effects are very important, leading to a partial suppression of the occurrence of magic numbers, as well as to low-symmetry and less compact clusters.

In general, the IR bond gives information about the point group symmetry of structures [62, 63]. Bonds that are formed in the near-infra-red range are considered the weaker ones. Far infrared spectroscopy is observed in the frequency region that is less than 10 cm^{-1} and responds to the stretching and bending mode of vibrations. In the experiment, generally not able to observe the silent modes that play a fundamental role in the intermolecular non-radiative energy transfer of energy and play a central role in the determination of stability of the gold clusters [30].

For the perspective view, we have plotted with two different styles (Space-filling, Polyhedral). Specifically, Figures 1-10, sharply show the standard orientation of the crystal shape of the clusters Au_{26-35} at $\Delta E = 0$ (the lowest energy geometrical structure).

The vibrational frequency (ω_i) range of the cluster Au_{26} at $\Delta E = 0$

Table 1 shows the low (at the least) and the high (at the most) frequency range of the cluster Au_{26} , which occurs between 6.58 and 319.61 cm⁻¹, and the lowest energy geometrical structural view can be seen in Figure 1.

Firstly, the cluster has some low frequencies (ω_{min}) between 6.58 - 9.39 cm⁻¹, which is only for the very first 3 NVM that comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 4 - 58 NVM, the frequency ranges have occurred between 10.70 - 197.37 cm⁻¹, which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 59 - 72 NVM, is having the maximum high frequencies, which are ((ω_i) - 202.15 - 319.61 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{23.38, 23.71}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Certainly, such kind of spectrum could be highly possible to observe in the experimental calculations. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

Very recently, Fa Wei, and Jin-ming Dong [29] have shown the VDOS and corresponding FIR absorption spectrum of the lowest-energy tube-like Au_{26} . Yes, the vibration density of states (VDOS) was obtained by a convolution with a Lorentzian broadening of 2 cm⁻¹. They have shown in Figure 2 of their paper, the normal frequencies of the tube-like D_{6d} Au₂₆ locate in the range of 23 - 185 cm⁻¹. Only a portion of its vibration modes are infrared-active due to its high symmetry, and as a result, its far-infrared (FIR) spectrum exhibits some well-resolved peaks. They have had a hope that the infrared resonance-enhanced multiple photon dissociation measurements can be used to acquire the FIR absorption spectrum of Au₂₆, as those done for vanadium and niobium clusters [64 - 66], so that the existence of their tubelike $D_{6d} Au_{26}$ can be validated. In addition, they also noticed that the tube-like $D_{6d} Au_{26}$ has a radial breathing-like mode at 119

Table 1: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{26} at AE = 0

| $\Delta L = 0.$ | | | | | |
|-----------------|-------------------------------|------------|-------------------------------|------------|--------------------------------|
| NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | $\omega_i [\mathrm{cm}^{-1}]$ |
| 1 | 6.58 | 34 | 70.45 | 67 | 258.00 |
| 2 | 7.29 | 35 | 78.10 | 68 | 265.07 |
| 3 | 9.39 | 36 | 80.07 | 69 | 268.11 |
| 4 | 10.70 | 37 | 83.41 | 70 | 292.52 |
| 5 | 11.87 | 38 | 87.48 | 71 | 311.52 |
| 6 | 12.93 | 39 | 89.29 | 72 | 319.61 |
| 7 | 15.24 | 40 | 94.17 | 73 | - |
| 8 | 16.53 | 41 | 98.24 | 74 | - |
| 9 | 17.19 | 42 | 107.64 | 75 | - |
| 10 | 18.64 | 43 | 108.67 | 76 | - |
| 11 | 20.11 | 44 | 114.24 | 77 | - |
| 12 | 21.17 | 45 | 118.12 | 78 | - |
| 13 | 23.38 | 46 | 125.24 | 79 | - |
| 14 | 23.71 | 47 | 133.10 | 80 | - |
| 15 | 27.87 | 48 | 137.96 | 81 | - |
| 16 | 28.26 | 49 | 138.62 | 82 | - |
| 17 | 29.37 | 50 | 147.07 | 83 | - |
| 18 | 31.95 | 51 | 158.52 | 84 | - |
| 19 | 33.79 | 52 | 159.82 | 85 | - |
| 20 | 34.92 | 53 | 164.40 | 86 | - |
| 21 | 36.62 | 54 | 172.92 | 87 | - |
| 22 | 38.77 | 55 | 182.37 | 88 | - |
| 23 | 40.98 | 56 | 189.42 | 89 | - |
| 24 | 41.87 | 57 | 191.12 | 90 | - |
| 25 | 43.84 | 58 | 197.37 | 91 | - |
| 26 | 47.67 | 59 | 202.15 | 92 | - |
| 27 | 54.03 | 60 | 206.51 | 93 | - |
| 28 | 58.48 | 61 | 214.69 | 94 | - |
| 29 | 59.69 | 62 | 218.92 | 95 | - |
| 30 | 61.31 | 63 | 226.91 | 96 | - |
| 31 | 64.49 | 64 | 230.00 | 97 | - |
| 32 | 66.90 | 65 | 234.05 | 98 | - |
| 33 | 68.03 | 66 | 249.25 | 99 | - |
| | | | | | |





lowest energy geometrical structure of the Au_{26} cluster. Standard orientation of crystal shape at $\Delta E = 0$.

cm⁻¹, characteristic of the tube-like or cage structures, which is similar to radial breaking modes found in the carbon nanotubes, and so may be tested by future Raman spectra. Our calculated spectral range (refer to Tables 1-10) is in excellent agreement with theoretical and experimental predictions [29].

For larger sizes of n = 26-30, pyramidal motifs tend to dominate the lower-lying population rather than tubular conformations as previously reported. The energy gaps, excitation energies, and exciton binding energies were also computed to test out the performance of the computational methods employed. Accordingly, a density functional with long-range exchange effects was highly recommended to quantitatively investigate both the ground and excited states of pure gold clusters [67].

The vibrational frequency (ω_i) range of the cluster Au_{27} at $\Delta E = 0$

Table 2 shows the low (at the least) and the high (at the most) frequency range of the cluster Au_{27} , which occurs between 9.44 and 314.57 cm⁻¹, and the lowest energy geometrical structural view can be seen in Figure 2.

Firstly, the cluster has only one low frequency (ω_{min}) 9.44 cm⁻¹, which is only for the very first NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 2 - 59 NVM, the frequency ranges have occurred between 12.06 - 199.84 cm⁻¹, which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 60 - 75 NVM, is having the maximum high frequencies, which are ((ω_i) - 203.97 - 314.57 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{15.04, 15.67}; {22.31,

22.92}; {33.17, 33.90}; {83.22, 83.81} and {122.58, 122.99}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Certainly, such kind of spectrum could be highly possible to observe in the experimental calculations. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

Nhat PV, *et al.* have shown that many Au_{27} isomers were predicted to be energetically quasi-degenerate, the corresponding distinctive vibrational signatures could be used as fingerprints for the identification of cluster geometrical features [68].

New photoelectron spectroscopy (PES) data were obtained using Ar-seeded He supersonic beams to achieve better cluster cooling, resulting in well-resolved spectra and revealing the presence of low-lying isomers in a number of systems. Densityfunctional theory calculations were used for global minimum searches. For each cluster anion, more than 200 low-lying isomers are generated using the basin-hopping global minimum search algorithm. The most viable structures and low-lying isomers were obtained using both the relative energies and comparisons between the simulated spectra and experimental PES data [28].

Table 2: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{27} at

| $\Delta E = 0.$ | | | | | | | |
|-----------------|-------------------------------|------------|-------------------------------|------------|-------------------------------|--|--|
| NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | | |
| 1 | 9.44 | 34 | 83.22 | 67 | 252.37 | | |
| 2 | 12.06 | 35 | 83.81 | 68 | 262.49 | | |
| 3 | 13.02 | 36 | 87.41 | 69 | 268.77 | | |
| 4 | 15.04 | 37 | 90.60 | 70 | 269.62 | | |
| 5 | 15.67 | 38 | 94.95 | 71 | 277.72 | | |
| 6 | 17.84 | 39 | 103.39 | 72 | 279.89 | | |
| 7 | 18.03 | 40 | 109.89 | 73 | 293.66 | | |
| 8 | 20.13 | 41 | 112.30 | 74 | 305.85 | | |
| 9 | 22.31 | 42 | 115.90 | 75 | 314.57 | | |
| 10 | 22.92 | 43 | 122.58 | 76 | - | | |
| 11 | 24.14 | 44 | 122.99 | 77 | - | | |
| 12 | 26.28 | 45 | 130.27 | 78 | - | | |
| 13 | 29.30 | 46 | 137.14 | 79 | - | | |
| 14 | 31.97 | 47 | 139.33 | 80 | - | | |
| 15 | 33.17 | 48 | 143.43 | 81 | - | | |
| 16 | 33.90 | 49 | 149.53 | 82 | - | | |
| 17 | 35.55 | 50 | 154.29 | 83 | - | | |
| 18 | 38.46 | 51 | 162.43 | 84 | - | | |
| 19 | 41.32 | 52 | 166.29 | 85 | - | | |
| 20 | 43.93 | 53 | 168.51 | 86 | - | | |
| 21 | 46.82 | 54 | 175.58 | 87 | - | | |
| 22 | 50.96 | 55 | 178.73 | 88 | - | | |
| 23 | 51.42 | 56 | 183.78 | 89 | - | | |
| 24 | 55.47 | 57 | 190.90 | 90 | - | | |
| 25 | 57.71 | 58 | 197.47 | 91 | - | | |
| 26 | 58.50 | 59 | 199.84 | 92 | - | | |
| 27 | 60.57 | 60 | 203.97 | 93 | - | | |
| 28 | 62.89 | 61 | 208.28 | 94 | - | | |
| 29 | 67.39 | 62 | 211.58 | 95 | - | | |
| 30 | 69.84 | 63 | 214.54 | 96 | - | | |
| 31 | 71.58 | 64 | 230.78 | 97 | - | | |
| 32 | 76.29 | 65 | 237.12 | 98 | - | | |
| 33 | 80.66 | 66 | 248.82 | 99 | - | | |





lowest energy geometrical structure of the Au_{27} cluster. Standard orientation of crystal shape at $\Delta E = 0$.

The global minimum structures of Au_n (n = 27, 28, 30, and 32-35) are found to exhibit low-symmetry core-shell structures with the number of core atoms increasing with cluster size: Au_{27} , Au_{28} , and Au_{30} possess a one-atom core; Au_{32} features a three-atom triangular core, and Au_{33} to Au_{35} all contain a four-atom tetrahedral core. The global searches reveal that the tetrahedral core is a popular motif for low-lying structures of Au_{33} to Au_{35} . The structural information forms the basis for future chemisorption studies to unravel the catalytic effects of gold nanoparticles [28].

The vibrational frequency (ω_i) range of the cluster Au_{28} at $\Delta E = 0$

Table 3 show the low (at the least) and the high (at the most) frequency range of the cluster Au_{28} , which occurs between 3.44 and 347.32 cm⁻¹, and the lowest energy geometrical structural view can be seen in Figure 3.

Firstly, the cluster has some low frequencies (ω_{min}) between 3.44 - 8.54 cm⁻¹, which is only for the very first 3 NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 4 - 62 NVM, the frequency ranges occurred between 10.69 - 195.49 cm⁻¹ which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 63 - 78 NVM, is having the maximum high frequencies, which are ((ω_i) - 202.34 - 347.32 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{11.19, 11.41}; {23.20, 23.72}; {30.21, 30.69}; {172.26, 172.82} and {177.05, 177.14}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Surely, such kind of spectrum could be highly possible to observe in the experimental

| $\Delta E = 0.$ | | | | | |
|-----------------|--------------------------------|------------|--------------------------------|------------|-------------------------------|
| NVM (3N-6) | $\omega_i [\mathrm{cm}^{-1}]$ | NVM (3N-6) | ω_i [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] |
| 1 | 3.44 | 34 | 71.90 | 67 | 223.32 |
| 2 | 5.97 | 35 | 74.57 | 68 | 224.94 |
| 3 | 8.54 | 36 | 75.35 | 69 | 234.57 |
| 4 | 10.69 | 37 | 80.47 | 70 | 245.19 |
| 5 | 11.19 | 38 | 82.57 | 71 | 248.60 |
| 6 | 11.41 | 39 | 89.17 | 72 | 261.29 |
| 7 | 13.34 | 40 | 94.30 | 73 | 265.51 |
| 8 | 14.74 | 41 | 96.39 | 74 | 276.00 |
| 9 | 16.02 | 42 | 101.25 | 75 | 285.42 |
| 10 | 17.35 | 43 | 103.42 | 76 | 300.57 |
| 11 | 18.26 | 44 | 109.54 | 77 | 336.31 |
| 12 | 22.09 | 45 | 113.33 | 78 | 347.32 |
| 13 | 23.20 | 46 | 117.44 | 79 | - |
| 14 | 23.72 | 47 | 119.48 | 80 | - |
| 15 | 26.59 | 48 | 121.17 | 81 | - |
| 16 | 27.73 | 49 | 127.25 | 82 | - |
| 17 | 30.21 | 50 | 131.03 | 83 | - |
| 18 | 30.69 | 51 | 137.09 | 84 | - |
| 19 | 33.85 | 52 | 142.67 | 85 | - |
| 20 | 35.23 | 53 | 148.05 | 86 | - |
| 21 | 37.24 | 54 | 150.42 | 87 | - |
| 22 | 39.26 | 55 | 153.40 | 88 | - |
| 23 | 40.33 | 56 | 164.08 | 89 | - |
| 24 | 43.62 | 57 | 172.26 | 90 | - |
| 25 | 45.31 | 58 | 172.82 | 91 | - |
| 26 | 49.10 | 59 | 177.05 | 92 | - |
| 27 | 50.90 | 60 | 177.14 | 93 | - |
| 28 | 55.10 | 61 | 190.90 | 94 | - |
| 29 | 57.50 | 62 | 195.49 | 95 | - |
| 30 | 58.48 | 63 | 202.34 | 96 | - |
| 31 | 61.40 | 64 | 207.69 | 97 | - |
| 32 | 64.27 | 65 | 213.68 | 98 | - |
| 33 | 67.89 | 66 | 218.24 | 99 | - |

Table 3: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au₂₈ at



Figure 3: Au₂₈ (C₁); Style (Space-filling [top], Polyhedral [bottom]): The lowest energy geometrical structure of the Au₂₈ cluster. Standard orientation of crystal shape at $\Delta E = 0$.



calculations. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the two different elliptical motions but that could be a single motion as an individual.

The global minimum structures of Au_{n} (n = 27, 28, 30, and 32-35) are found to exhibit low-symmetry core-shell structures with the number of core atoms increasing with cluster size: Au_{27} , Au_{28} , and Au_{30} possess a one-atom core; Au_{32} features a three-atom triangular core, and Au_{33} to Au_{35} all contain a four-atom tetrahedral core. The global searches reveal that the tetrahedral core is a popular motif for low-lying structures of Au_{33} to Au_{35} . The structural information forms the basis for future chemisorption studies to unravel the catalytic effects of gold nanoparticles [28].

Applications: The recently reported crystal structure of the $Au_{28}(\text{TBBT})_{20}$ cluster (TBBT: p-test-butylbenzenethiolate) was analyzed with (time-dependent) density functional theory (TD-DFT). Bader charge analysis reveals a novel trimeric $Au_3(\text{SR})_4$ binding motif. The cluster can be formulated as $Au_{14}((\text{SR})_3)_4(Au_3(\text{SR})_4)_2$. The electronic structure of the Au_{14}^{6+} core and the ligand-protected cluster were analyzed, and their stability could be explained by the formation of distorted eight-electron superatoms. Optical absorption and circular dichroism (CD) spectra were calculated and compared to the experiment. Assignment of handedness of the intrinsically chiral cluster is possible [69].

Wang, Shuxin, *et al.* substituted gold atoms in fcc-structured Au_{28} and Au_{36} nanoclusters with Ag(I)SR complex and obtained Ag_xAu_{28-x} and Ag_xAu_{36-x} nanoclusters, respectively [70]. Lin Xiong, *et al.* proposed a novel 'gold-atom insertion, thiolate-group elimination' mechanism to understand the structural evolution of the face-centered-cubic (fcc) thiolate-protected gold clusters. The key step of structural evolution from $Au_{28}(SR)_{20}$ to $Au_{29}(SR)_{19}$ and then to the $Au_{30}(SR)_{18}$ cluster, *i.e.* the growth of triangle- Au_3 units in the gold cores, is understood from the first insertion of an exterior Au(0) atom into the ligand shell and then cleavage of μ_3 -SR groups [71-80].

The vibrational frequency (ω_i) range of the cluster Au_{29} at $\Delta E = 0$

Table 4 shows the low (at the least) and the high (at the most) frequency range of the cluster Au_{29} , which occurs between 2.34 and 315.87 cm⁻¹, and the lowest energy geo-metrical structural view can be seen in Figure 4.

Firstly, the cluster has some low frequencies (ω_{min}) between 2.34 - 9.74 cm⁻¹, which is only for the very first 4 NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 5 - 66 NVM, the frequency ranges occurred between 10.61 - 197.10 cm⁻¹ which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 67 - 81 NVM, is having the maximum high frequencies, which are ((ω_i) - 200.41 - 315.87 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

| $\Delta E = 0.$ | ·· [=17 | NIVING (2NL-C) | | NIX/NA (2NI-C) | |
|-----------------|-------------------------------|----------------|-----------------------------|----------------|-----------------------------|
| NVM (3N-6) | $\omega_i [\mathrm{cm}^{-1}]$ | NVM (3N-6) | $\omega_i [\text{cm}^{-1}]$ | NVM (3N-6) | $\omega_i [\text{cm}^{-1}]$ |
| 1 | 2.34 | 34 | 58.62 | 67 | 200.41 |
| 2 | 7.17 | 35 | 63.19 | 68 | 204.60 |
| 3 | 8.77 | 36 | 64.30 | 69 | 209.86 |
| 4 | 9.74 | 37 | 66.58 | 70 | 216.89 |
| 5 | 10.61 | 38 | 69.46 | 71 | 219.69 |
| 6 | 12.31 | 39 | 75.90 | 72 | 229.33 |
| 7 | 12.95 | 40 | 79.01 | 73 | 232.74 |
| 8 | 13.57 | 41 | 80.65 | 74 | 234.88 |
| 9 | 15.55 | 42 | 81.66 | 75 | 256.95 |
| 10 | 16.83 | 43 | 83.94 | 76 | 260.46 |
| 11 | 18.10 | 44 | 90.55 | 77 | 271.39 |
| 12 | 20.26 | 45 | 94.55 | 78 | 276.27 |
| 13 | 22.51 | 46 | 99.38 | 79 | 290.94 |
| 14 | 25.72 | 47 | 101.05 | 80 | 309.20 |
| 15 | 26.12 | 48 | 105.21 | 81 | 315.87 |
| 16 | 28.37 | 49 | 109.42 | 82 | - |
| 17 | 30.33 | 50 | 110.81 | 83 | - |
| 18 | 31.33 | 51 | 115.14 | 84 | - |
| 19 | 32.49 | 52 | 115.67 | 85 | - |
| 20 | 32.91 | 53 | 122.96 | 86 | - |
| 21 | 35.43 | 54 | 125.73 | 87 | - |
| 22 | 36.89 | 55 | 127.15 | 88 | - |
| 23 | 38.12 | 56 | 133.96 | 89 | - |
| 24 | 39.02 | 57 | 140.95 | 90 | - |
| 25 | 40.44 | 58 | 143.66 | 91 | - |
| 26 | 43.84 | 59 | 147.50 | 92 | - |
| 27 | 44.76 | 60 | 150.01 | 93 | - |
| 28 | 46.73 | 61 | 154.13 | 94 | - |
| 29 | 48.18 | 62 | 159.19 | 95 | - |
| 30 | 49.86 | 63 | 173.21 | 96 | - |
| 31 | 50.97 | 64 | 180.20 | 97 | - |
| 32 | 54.91 | 65 | 183.92 | 98 | - |
| 33 | 56.74 | 66 | 197.10 | 99 | - |
| | | | | | |

Table 4: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{29} at





The double state degeneracy, ω_i : [{12.31, 12.95}; {32.49, 32.91} and {115.14, 115.67}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Surely, such kind of spectrum could be highly possible to observe in the experimental calculations, except the first pair can be in silent mode. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

Applications: The atomic structure of a ten-electron (10e) thiolate-protected gold cluster, denoted as $Au_{29}(SR)_{19}$, was theoretically predicted. Based on the prediction of the atomic structure of the 10e $Au_{29}(SR)_{19}$ cluster, Lin Xiong, *et al.* proposed a novel 'gold-atom insertion, thiolate-group elimination' mechanism to understand the structural evolution of the face-centered-cubic (fcc) thiolate-protected gold clusters. The key step of structural evolution from $Au_{28}(SR)_{20}$ to $Au_{29}(SR)_{19}$ and then to the $Au_{30}(SR)_{18}$ cluster, *i.e.* the growth of triangle- Au_3 units in the gold cores, is understood from the first insertion of an exterior Au(0) atom into the ligand shell and then cleavage of μ_3 -SR groups [71].

The vibrational frequency (ω_i) range of the cluster Au_{30} at $\Delta E = 0$

Table 5 shows the low (at the least) and the high (at the most) frequency ranges of the cluster Au_{30} , which are 2.35 and 308.09 cm⁻¹, and the lowest energy geometrical structural view can be seen in Figure 5.

Firstly, the cluster has some low frequencies (ω_{min}) between 2.35 - 9.59 cm⁻¹, which is only for the very first 3 NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 4 - 69 NVM, the frequency ranges have occurred between 11.30 - 197.11 cm⁻¹ which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 70 - 84 NVM, is having the maximum high frequencies, which are ((ω_i) - 200.82 - 308.09 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{15.19, 15.30}; {23.33, 23.65}; {28.26, 28.73} and {37.05, 37.41}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Certainly, such kind of spectrum could be highly possible to observe in the experimental calculations, except for the first pair. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

Structural evolution and stability pattern of pure neutral gold clusters Au_n in the small size range of n = 20-30 are examined using density functional theory (DFT) calculations. The equilibrium geometries are either confirmed or deter-mined, and some new ground state structures are identified [67].

For larger sizes of n = 26-30, pyramidal motifs tend to

| $\Delta E = 0.$ | | | | | |
|-----------------|--------------------------------|------------|-------------------------------|------------|-------------------------------|
| NVM (3N-6) | $\omega_i [\mathrm{cm}^{-1}]$ | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] |
| 1 | 2.35 | 34 | 62.49 | 67 | 184.57 |
| 2 | 7.12 | 35 | 63.91 | 68 | 194.04 |
| 3 | 9.59 | 36 | 65.16 | 69 | 197.11 |
| 4 | 11.30 | 37 | 71.33 | 70 | 200.82 |
| 5 | 15.19 | 38 | 73.45 | 71 | 206.02 |
| 6 | 15.30 | 39 | 75.64 | 72 | 210.31 |
| 7 | 16.84 | 40 | 79.01 | 73 | 213.54 |
| 8 | 17.32 | 41 | 80.25 | 74 | 216.10 |
| 9 | 19.03 | 42 | 82.19 | 75 | 221.37 |
| 10 | 22.45 | 43 | 86.13 | 76 | 229.18 |
| 11 | 23.33 | 44 | 89.52 | 77 | 235.60 |
| 12 | 23.65 | 45 | 94.13 | 78 | 238.08 |
| 13 | 26.05 | 46 | 96.64 | 79 | 243.49 |
| 14 | 27.40 | 47 | 98.86 | 80 | 245.67 |
| 15 | 28.26 | 48 | 104.04 | 81 | 249.27 |
| 16 | 28.73 | 49 | 109.05 | 82 | 260.68 |
| 17 | 31.56 | 50 | 112.34 | 83 | 261.88 |
| 18 | 33.09 | 51 | 114.20 | 84 | 308.09 |
| 19 | 35.11 | 52 | 118.35 | 85 | - |
| 20 | 37.05 | 53 | 124.72 | 86 | - |
| 21 | 37.41 | 54 | 131.18 | 87 | - |
| 22 | 39.69 | 55 | 132.85 | 88 | - |
| 23 | 41.21 | 56 | 140.38 | 89 | - |
| 24 | 42.88 | 57 | 143.58 | 90 | - |
| 25 | 43.55 | 58 | 147.90 | 91 | - |
| 26 | 45.68 | 59 | 149.98 | 92 | - |
| 27 | 47.59 | 60 | 158.29 | 93 | - |
| 28 | 48.91 | 61 | 161.01 | 94 | - |
| 29 | 52.46 | 62 | 163.96 | 95 | - |
| 30 | 53.71 | 63 | 171.15 | 96 | - |
| 31 | 56.04 | 64 | 172.52 | 97 | - |
| 32 | 57.80 | 65 | 176.91 | 98 | - |
| 33 | 61.16 | 66 | 182.65 | 99 | - |
| | | 1 | | | |

Table 5: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{30} at



Figure 5: Au_{30} (C_1); Style (Space-filling [top], Polyhedral [bottom]): The lowest energy geometrical structure of the Au_{30} cluster. Standard orientation of crystal shape at $\Delta E = 0$.



dominate the lower-lying population rather than tubular conformations as previously reported. The energy gaps, excitation energies, and exciton binding energies were also computed to test out the performance of the computational methods employed. Accordingly, a density functional with long-range exchange effects was highly recommended to quantitatively investigate both the ground and excited states of pure gold clusters [67].

The vibrational frequency (ω_i) range of the cluster Au_{31} at $\Delta E = 0$

Table 6 shows the low (at the least) and the high (at the most) frequency range of the cluster Au_{31} , which occurs between 8.98 and 322.69 cm⁻¹, and the lowest energy geometrical structural view can be seen in Figure 6.

Firstly, the cluster has a low frequency (ω_{min}) of 8.98 cm⁻¹ which is only for the very first NVM which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 2 - 69 NVM, the frequency ranges occurred between 11.12 - 195.72 cm⁻¹ which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 70 - 87 NVM, is having the maximum high frequencies, which are ((ω_i) - 204.28 - 322.69 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{11.12, 11.18}; {32.49, 32.87}; {46.62, 46.98}; {66.56, 66.77}; {148.02, 148.35} and {195.09, 195.92}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Surely, such kind of spectrum could be highly possible to observe in the experimental calculations, except for the first two pairs that can be in silent modes. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

The structural evolution of negatively charged gold clusters (Au_n^-) in the medium size range for n = 27-35 has been investigated using photoelectron spectroscopy (PES) and theoretical calculations [28]. Nonetheless, at present, we do not find any literature that compares with our results!

The vibrational frequency (ω_i) range of the cluster Au_{32} at $\Delta E = 0$

Table 7 shows the low (at the least) and the high (at the most) frequency range of the cluster Au_{32} , which occurs between 2.43 and 341.62 cm⁻¹, and the lowest energy geo-metrical structural view can be seen in Figure 7.

Firstly, the cluster has some low frequencies (ω_{min}) between 2.43 - 8.07 cm⁻¹ which is only for the very first 4 NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 5 - 74 NVM, the frequency ranges occurred between 10.51 - 196.16 cm⁻¹ which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 75 - 90 NVM, is having the maximum high frequencies, which

| $\Delta E = 0.$ | | | | | | |
|-----------------|-------------------------------|------------|-------------------------------|------------|-------------------------------|--|
| NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | |
| 1 | 8.98 | 34 | 66.56 | 67 | 191.59 | |
| 2 | 11.12 | 35 | 66.77 | 68 | 195.09 | |
| 3 | 11.18 | 36 | 70.96 | 69 | 195.92 | |
| 4 | 13.26 | 37 | 72.24 | 70 | 204.28 | |
| 5 | 14.19 | 38 | 75.16 | 71 | 206.91 | |
| 6 | 16.25 | 39 | 80.71 | 72 | 210.89 | |
| 7 | 18.51 | 40 | 81.75 | 73 | 215.13 | |
| 8 | 19.97 | 41 | 82.84 | 74 | 217.46 | |
| 9 | 21.76 | 42 | 84.77 | 75 | 221.26 | |
| 10 | 22.38 | 43 | 91.92 | 76 | 225.02 | |
| 11 | 23.43 | 44 | 94.11 | 77 | 236.70 | |
| 12 | 24.52 | 45 | 97.52 | 78 | 240.50 | |
| 13 | 25.70 | 46 | 99.67 | 79 | 246.18 | |
| 14 | 27.62 | 47 | 103.65 | 80 | 252.30 | |
| 15 | 28.51 | 48 | 106.13 | 81 | 255.31 | |
| 16 | 31.70 | 49 | 110.95 | 82 | 263.87 | |
| 17 | 32.49 | 50 | 114.51 | 83 | 266.21 | |
| 18 | 32.87 | 51 | 116.98 | 84 | 270.82 | |
| 19 | 34.40 | 52 | 120.17 | 85 | 288.83 | |
| 20 | 36.42 | 53 | 126.07 | 86 | 296.43 | |
| 21 | 38.92 | 54 | 129.44 | 87 | 322.69 | |
| 22 | 39.55 | 55 | 138.09 | 88 | - | |
| 23 | 41.52 | 56 | 142.91 | 89 | - | |
| 24 | 43.39 | 57 | 148.02 | 90 | - | |
| 25 | 46.62 | 58 | 148.35 | 91 | - | |
| 26 | 46.98 | 59 | 159.85 | 92 | - | |
| 27 | 51.29 | 60 | 161.99 | 93 | - | |
| 28 | 52.42 | 61 | 163.55 | 94 | - | |
| 29 | 54.99 | 62 | 167.68 | 95 | - | |
| 30 | 55.54 | 63 | 168.97 | 96 | - | |
| 31 | 57.30 | 64 | 171.15 | 97 | - | |
| 32 | 59.46 | 65 | 177.58 | 98 | - | |
| 33 | 61.97 | 66 | 183.57 | 99 | - | |

Table 6: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{31} at



Figure 6: Au_{31} (C_1); Style (Space-filling [top], Polyhedral [bottom]): The lowest energy geometrical structure of the Au_{31} cluster. Standard orientation of crystal shape at $\Delta E = 0$.



| Table 7: The N $\Delta E = 0.$ | Normal modes | (NVM) and the | vibrational | frequencies (ω_i) | of Au_{32} at |
|--|--------------------------------|---------------|-------------------------------|--------------------------|-------------------------------|
| NVM (3N-6) | ω_i [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] |
| 1 | 2.43 | 34 | 54.40 | 67 | 164.78 |
| 2 | 5.32 | 35 | 58.71 | 68 | 169.04 |
| 3 | 6.65 | 36 | 60.02 | 69 | 172.13 |
| 4 | 8.07 | 37 | 61.26 | 70 | 174.38 |
| 5 | 10.51 | 38 | 64.86 | 71 | 179.49 |
| 6 | 12.03 | 39 | 66.81 | 72 | 189.59 |
| 7 | 13.63 | 40 | 69.41 | 73 | 192.77 |
| 8 | 14.78 | 41 | 69.79 | 74 | 196.16 |
| 9 | 17.01 | 42 | 70.50 | 75 | 201.19 |
| 10 | 17.54 | 43 | 76.24 | 76 | 208.44 |
| 11 | 19.98 | 44 | 77.65 | 77 | 214.56 |
| 12 | 21.73 | 45 | 80.59 | 78 | 215.82 |
| 13 | 23.01 | 46 | 82.74 | 79 | 217.55 |
| 14 | 23.77 | 47 | 84.60 | 80 | 222.58 |
| 15 | 24.16 | 48 | 86.68 | 81 | 226.53 |
| 16 | 25.51 | 49 | 89.34 | 82 | 236.59 |
| 17 | 27.03 | 50 | 91.93 | 83 | 239.92 |
| 18 | 29.02 | 51 | 95.23 | 84 | 244.35 |
| 19 | 31.37 | 52 | 101.36 | 85 | 247.90 |
| 20 | 32.43 | 53 | 104.59 | 86 | 254.41 |
| 21 | 33.29 | 54 | 105.93 | 87 | 269.72 |
| 22 | 34.83 | 55 | 111.54 | 88 | 284.47 |
| 23 | 36.10 | 56 | 114.46 | 89 | 293.94 |
| 24 | 37.10 | 57 | 115.17 | 90 | 341.62 |
| 25 | 38.54 | 58 | 124.16 | 91 | - |
| 26 | 41.59 | 59 | 132.79 | 92 | - |
| 27 | 43.69 | 60 | 136.77 | 93 | - |
| 28 | 45.11 | 61 | 139.20 | 94 | - |
| 29 | 46.73 | 62 | 146.23 | 95 | - |
| 30 | 47.66 | 63 | 147.91 | 96 | - |
| 31 | 49.36 | 64 | 152.56 | 97 | - |
| 32 | 50.93 | 65 | 157.23 | 98 | - |
| 33 | 53.01 | 66 | 164.25 | 99 | - |



Figure 7: $Au_{32}(C_1)$; Style (Space-filling [top], Polyhedral [bottom]): The lowest energy geometrical structure of the Au_{32} cluster. Standard orientation of crystal shape at $\Delta E = 0$.

are ((ω_i) - 201.19 - 341.62 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{17.01, 17.54}; {23.01, 23.77}; {69.41, 69.79} and {164.25, 164.78}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Surely, such kind of spectrum could be highly possible to observe in the experimental calculations, except the first three pairs can be in a silent mode. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

More recently, a DFT study predicted the existence of the highly stable icosahedron Au_{32} cage, constructed from the carbon fullerene C_{60} as a template and so referred to as "golden" fullerene [72, 73]. The Au_{32} fullerene cage satisfies the $2(N+1)^2$ aromatic rule [74] and has an extremely large energy gap between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) up to at least 1.5 eV, showing its chemical stability and its potential ability to assemble into molecular crystals. Furthermore, Gao, *et al.* and Fa W, *et al.* have used the BP86 method recently study the Au_{32} with the DFT relativistic effects and cage-like structure and that was stable chemically and ground state due to the extremely larger bandgap between the HOMO and the LUMO that was approximately up to the 1.7 eV [75, 76].

Firstly, for the Gold cluster Au_{32} in which the numbers of atoms are 32 and it represents the mode at 122.339 cm⁻¹ with the IR Intensity 1.3387 km/mol. Secondly, for the Gold cluster Au_{32} in which the numbers of atoms are 32 and it represents two modes at the 134.70 cm⁻¹ and 1.2958 cm⁻¹ with the Partial IR Intensity 1.3387 km/mol and 0.003585 km/mol respectively [30].

Although we are not able to compare our results directly with Tahir Iqbal, *et al.* (The IR Intensity spectra for the gold cluster calculated via DFTB), but possible to compare with the highest amplitude of Au_n (n = 32) that is closely matched with our NVM 58, 59 and 60 that and the corresponding observed vibrational spectra's are 124.16, 132.79 and 136.77 cm⁻¹ respectively, which is a very good agreement with their results, having the reason with respect to our theoretical setup [30].

Ji, *et al.* first reported that Au_{32} - is a core-shell cluster with a three-atom triangular core. Further first-principals calculations suggested that the global minimum of Au_{32} - contains a fouratom tetrahedral core [31]. Certainly, neutral Au_{32} was reported to possess an icosahedral cage structure, a combined DFT and PES study showed that the Au_{32} - cluster anion possesses a more compact core-shell-type structure. Subsequent theoretical calculations support this conclusion [28].

In total, DFT calculations were carried out on bare Au_{32} and Au_{33} nanoclusters with various charges, in order to analyze their stability with respect to different cluster electron numbers. Results indicated that in addition to the neutral Au_{32} hollow species,



significant HOMO-LUMO gaps were computed for $[Au_{32}]^{8+}$ (hollow) and $[Au_{32}]^{4+}$ (two-shell structure). Species with smaller HOMO-LUMO gaps can reach stability upon "passivation" by a ligand shell, as experimentally exemplified. Icosahedral frameworks of Ih or lower symmetry are favored for the cationic nanoclusters whereas different structures are computed for the anionic ones [26].

The vibrational frequency (ω_i) range of the cluster Au_{33} at $\Delta E = 0$

Table 8 shows the low (at the least) and the high (at the most) frequency range of the cluster Au_{33} , which occurs between 5.49 and 284.91 cm⁻¹, and the lowest energy geo-metrical structural view can be seen in Figure 8.

Firstly, the cluster has some low frequencies (ω_{min}) between 5.49 - 7.86 cm⁻¹ which is only for the very first 3 NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 4 - 71 NVM, the frequency ranges occurred between 12.13 - 192.37 cm⁻¹ which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 72 - 93 NVM, is having the maximum high frequencies, which are ((ω_i) - 201.44 - 284.91 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{5.49, 5.79}; {17.23, 17.39}; {24.33 24.74}; {25.16, 25.75}; {27.75, 27.94}; {30.08, 30.70}; {64.36, 64.58}; {72.24; 72.58}; {192.00, 192.37}; {216.03, 216.91}; {221.56, 221.91}; {240.10, 240.86}; {261.02, 261.80} and {284.36, 284.91}] in cm⁻¹. The degree of degeneracy has occurred below, as well as within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹ and also falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹. Surely, such kind of spectrum could be highly possible to observe in the experimental calculations, except the first two pairs can be in a silent mode. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

A Special structure of Au_{33} (D_2): The excellencies of these clusters are having much and full of double-state degeneracy, apart from this, cluster Au₃₃ has many interesting futures; one is, the spectral pair begins at the first two NVM {1, 2} itself, as well as, it ends with the extreme last two NVM {92, 93}, and the second one is, some of the pairs have degenerated consecutively (that will help for rapid degenerate rearrangements of a chemical species), in addition to that, 30.10% spectral covered fully with double pairs in the same level and are all equally probable of being filled, and the rest of them are having single degenerate states, and also the presence of some symmetry in the system, additionally the radial distances of the interatomic distances also plays a major role. Interesting things to be noticed, having 5d and 6s valance electrons per gold atom, the nuclei were smeared out of a spherical medium (jellium), with a constant density inside, which the valence electrons were moving.

| $\Delta L = 0.$ | | | | | |
|-----------------|-------------------------------|------------|-------------------------------|------------|-------------------------------|
| NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] |
| 1 | 5.49 | 34 | 59.26 | 67 | 175.57 |
| 2 | 5.79 | 35 | 60.36 | 68 | 176.52 |
| 3 | 7.86 | 36 | 62.09 | 69 | 177.82 |
| 4 | 12.13 | 37 | 64.36 | 70 | 192.00 |
| 5 | 13.71 | 38 | 64.58 | 71 | 192.37 |
| 6 | 15.46 | 39 | 66.77 | 72 | 201.44 |
| 7 | 16.61 | 40 | 72.24 | 73 | 207.91 |
| 8 | 17.23 | 41 | 72.58 | 74 | 216.03 |
| 9 | 17.39 | 42 | 75.87 | 75 | 216.91 |
| 10 | 20.96 | 43 | 76.48 | 76 | 221.56 |
| 11 | 21.37 | 44 | 85.68 | 77 | 221.91 |
| 12 | 22.02 | 45 | 87.70 | 78 | 222.20 |
| 13 | 23.83 | 46 | 94.32 | 79 | 235.78 |
| 14 | 24.33 | 47 | 95.52 | 80 | 237.35 |
| 15 | 24.74 | 48 | 96.22 | 81 | 240.10 |
| 16 | 25.16 | 49 | 100.89 | 82 | 240.86 |
| 17 | 25.75 | 50 | 101.17 | 83 | 241.52 |
| 18 | 26.79 | 51 | 110.61 | 84 | 249.37 |
| 19 | 27.75 | 52 | 111.12 | 85 | 250.62 |
| 20 | 27.94 | 53 | 112.08 | 86 | 252.65 |
| 21 | 29.45 | 54 | 116.55 | 87 | 261.02 |
| 22 | 30.08 | 55 | 117.16 | 88 | 261.80 |
| 23 | 30.70 | 56 | 127.62 | 89 | 266.83 |
| 24 | 31.34 | 57 | 140.31 | 90 | 270.59 |
| 25 | 33.06 | 58 | 141.84 | 91 | 273.37 |
| 26 | 34.09 | 59 | 142.33 | 92 | 284.36 |
| 27 | 36.38 | 60 | 145.48 | 93 | 284.91 |
| 28 | 37.96 | 61 | 147.97 | 94 | - |
| 29 | 45.91 | 62 | 151.88 | 95 | - |
| 30 | 46.80 | 63 | 152.00 | 96 | - |
| 31 | 47.08 | 64 | 158.56 | 97 | - |
| 32 | 54.45 | 65 | 159.32 | 98 | - |
| 33 | 58.84 | 66 | 163.22 | 99 | - |
| | | | | | |

Table 8: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{33} at



Figure 8: Au_{33} (D_2); Style (Space-filling [top], Polyhedral [bottom]): The lowest energy geometrical structure of the Au_{33} cluster. Standard orientation of crystal shape at $\Delta E = 0$.



The results of DFT calculations by Gu, *et al.* [36, 73] on Au_N Clusters with $32 \le N \le 35$ point to the existence of cage-like structures. Fa, *et al.* [76] suggested that the possible occurrences of the structures related to either fragment of the crystal or to tubelike structures. These tube-like Au_n with larger surface area and hollow inner space may be important for fundamental chemistry researches, and in the future, have a wide range of applications in catalysis, biology, nanotechnology.

The orbitals have much lower degeneracy in the DFTB calculations leading to many more, different orbital energies. A very remarkable exception is N = 33 which has only a few different orbital energies and, in addition, is particularly stable. Moreover, we predict that the cluster for N = 33 is particularly stable and symmetric, the reason could be, such kind of clusters often possess their atoms on the surface of the compact core that is bonded (for covalently bonded elements, the effects due to directional bonds are dominating) to only one or two nearest neighbors, that is one of the main reasons, that our re-optimized structures do not have a very high symmetry (when including orbital interactions). Most significantly, lower nuclear charge effects on the neighboring electrons drive the greater change of electron density that causes the rise of the bond distance due to vibration stimulation and these changes in vibrations are the fundamental interest in Raman spectroscopy. Various experimental studies are reported for molecular scale in the literature that exploits the optical spectra, high polarizability, and emission properties of the noble metal clusters [77 - 80].

Supporting information: It is all shown through two different types of structural views: The first one is, a view along the a, b, and c axis and also a view along the a^* , b^* , and c^* axis (Figures 8a-f). The second one is, to rotate around the x-axis (upward direction) and to rotate around the x-axis (downward direction); to rotate around the y-axis (left side direction) and to rotate around the z-axis (clockwise direction) and to rotate around the z-axis (anti-clockwise direction) (Figures 8A-F).

Of course, it is interesting to seek other non-space-filled gold clusters as potential true ground states for the bigger sizes. Therefore, further computational efforts are still needed to explore the energy landscapes of these medium-sized gold clusters. Nonetheless, Au_{33} prefers a highly symmetric tube-like structure without core atoms!

In particular, the figure shows that the Au_{33} cluster is exceptional and different from the other ones (Please refer, to the Supporting Information and the title of Figures 8 a-f and Figures 8 A-F).

Figure G: Clusters Au_{26-35} vs. the total number of pairs (the double-state degeneracy).

The vibrational frequency (ω_i) range of the cluster Au_{34} at $\Delta E = 0$

Table 9 shows the low (at the least) and the high (at the most)



frequency range of the cluster Au_{34} , which occurs between 5.06 and 322.42 cm⁻¹, and the lowest energy geo-metrical structural view can be seen in Figure 9.

Firstly, the cluster has some low frequencies (ω_{min}) between 5.06 - 8.47 cm⁻¹ which is only for the very first 4 NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 5 - 78 NVM, the frequency ranges occurred between 10.54 - 192.60 cm⁻¹ which comes within the range of Far

Table 9: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{34} at $\Delta E = 0$.

| $\Delta E = 0.$ | | | | | |
|-----------------|-------------------------------|------------|-------------------------------|------------|-------------------------------|
| NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] |
| 1 | 5.06 | 34 | 53.66 | 67 | 142.84 |
| 2 | 6.12 | 35 | 56.76 | 68 | 152.88 |
| 3 | 7.54 | 36 | 57.13 | 69 | 156.98 |
| 4 | 8.47 | 37 | 58.61 | 70 | 158.99 |
| 5 | 10.54 | 38 | 62.00 | 71 | 164.54 |
| 6 | 10.78 | 39 | 63.25 | 72 | 169.82 |
| 7 | 13.04 | 40 | 66.12 | 73 | 174.83 |
| 8 | 14.25 | 41 | 67.80 | 74 | 177.84 |
| 9 | 15.33 | 42 | 68.31 | 75 | 184.60 |
| 10 | 16.19 | 43 | 70.21 | 76 | 185.74 |
| 11 | 17.28 | 44 | 73.75 | 77 | 187.84 |
| 12 | 19.44 | 45 | 75.44 | 78 | 192.60 |
| 13 | 19.72 | 46 | 77.38 | 79 | 201.66 |
| 14 | 21.41 | 47 | 81.84 | 80 | 204.09 |
| 15 | 23.41 | 48 | 85.36 | 81 | 207.32 |
| 16 | 26.66 | 49 | 87.24 | 82 | 210.44 |
| 17 | 27.56 | 50 | 91.13 | 83 | 212.87 |
| 18 | 28.69 | 51 | 93.57 | 84 | 220.44 |
| 19 | 30.70 | 52 | 96.47 | 85 | 225.24 |
| 20 | 31.79 | 53 | 96.58 | 86 | 230.25 |
| 21 | 32.80 | 54 | 100.27 | 87 | 232.29 |
| 22 | 34.03 | 55 | 104.18 | 88 | 234.00 |
| 23 | 35.19 | 56 | 107.47 | 89 | 243.87 |
| 24 | 36.08 | 57 | 108.79 | 90 | 244.46 |
| 25 | 38.08 | 58 | 115.11 | 91 | 252.96 |
| 26 | 39.76 | 59 | 115.75 | 92 | 255.44 |
| 27 | 41.61 | 60 | 117.87 | 93 | 265.64 |
| 28 | 42.39 | 61 | 126.48 | 94 | 279.82 |
| 29 | 46.67 | 62 | 129.24 | 95 | 285.13 |
| 30 | 48.23 | 63 | 132.08 | 96 | 322.42 |
| 31 | 49.01 | 64 | 135.07 | 97 | - |
| 32 | 50.11 | 65 | 136.76 | 98 | - |
| 33 | 53.13 | 66 | 142.45 | 99 | - |
| 33 | 53.13 | 66 | 142.45 | 99 | - |





Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 79 - 96 NVM, is having the maximum high frequencies, which are ((ω_i) - 201.66 - 322.42 cm⁻¹) falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{10.54, 10.78}; {19.44, 19.72}; {53.13, 53.66}; {96.47, 96.58}; {115.11, 115.75} and {142.45, 142.84}] in cm⁻¹. The degree of degeneracy has occurred within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Surely, such kind of spectrum could be highly possible to observe in the experimental calculations. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

Xiao Gu, et al. [81], have confirmed that among the large Au_n clusters for n > 20, the photoelectron spectra of Au_{34} exhibit the largest energy gap (0.94 eV) with well-resolved spectral features, making it a good candidate for structural consideration in conjunction with theoretical studies. Extensive structural searches at several levels of density functional and ab initio theory revealed that the low-lying isomers of Au_{34} can be characterized as fluxional core-shell type structures with 4 or 3 inner atoms and 30 or 31 outer atoms, *i.e.*, $Au_4(a)Au_{30}$ and $Au_3(a)Au_{31}$, respectively. Detailed comparisons between theoretical and photoelectron results suggest that the most probable ground state structures of Au_{34} are of the $Au_4(a)Au_{30}$ type. The 30 outer atoms seem to be disordered or fluxional, giving rise to a number of low-lying isomers with very close energies and simulated photoelectron spectra. The fluxional nature of the outer layer in large gold clusters or nanoparticles may have important implications for their remarkable catalytic activities [81].

Itzel E. Santizo, et al. provided theoretical evidence for the existence of energetically stable chiral structures for bare gold clusters. Density functional theory calculations within the generalized-gradient approximation were performed to systematically study structural, vibrational, electronic, and optical properties of the lowest-lying isomers of the Au_{34}^{Z} , (Z = +1, 0, -1), clusters. Their results show that for the neutral and charged clusters, the lowest-energy isomer has a C_1 (chiral) structure. In addition, a C_3 (chiral) isomer was found to nearly degenerate in energy with the C_1 isomer. Those results are in agreement with previous theoretical-experimental studies done for the Au_{34}^{-} cluster; however, because their calculated molecular scattering functions for the C_1 and C_3 isomers of this cluster are almost indistinguishable, it is concluded that the actual resolution in trapped ion electron diffraction experiments was not enough to discriminate between them [82].

On the other hand, the electronic density of states of the C_1 isomer shows better overall agreement with the measured photoelectron spectrum of the Au_{34}^- cluster than that one corresponding to the C_3 isomer. The electronic density of states of these isomers also shows different features in the energy region of the HOMO-LUMO gap, which would generate distinct behavior in their optical properties. In fact, the calculated absorption and circular dichroism spectra of the two chiral isomers show clear differences in their line shape. Another important property that distinguishes the C_1 and C_3 isomers is the different spatial distribution of the atomic coordination on the cluster surface. Our results confirm that the potential energy surface (PES) of bare gold clusters could have the lowest-lying energy minima corresponding to intrinsically chiral structures [82].

In addition to that, the structures of the Au_{34} cluster have been studied both by TIED and PES, showing that its global minimum also consists of core-shell type structures with a fouratom core. For Au_{34} , the combined TIED and DFT study resulted in a C_3 core-shell cluster with a four-atom tetrahedral core, but the PES and DFT study found two low symmetry (C_1) core-shell structures, both with a four-atom tetrahedral core, competing for the global minimum. The low-symmetry C_1 structure for Au_{34} has been confirmed by two subsequent DFT studies [34 - 37, 81 - 83].

The vibrational frequency (ω_i) range of the cluster Au_{35} at $\Delta E = 0$

Table 10 shows the low (at the least) and the high (at the most) frequency range of the cluster Au_{35} , which occurs between 2.04 and 300.43 cm⁻¹, and the lowest energy geometrical structural view can be seen in Figure 10.

Firstly, the cluster has some low frequencies (ω_{min}) between 2.04 - 9.69 cm⁻¹ which is only for the very first 6 NVM, which comes even below the scale of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Secondly, for the 7 - 84 NVM, the frequency ranges occurred between 10.08 - 196.65 cm⁻¹ which comes within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Thirdly, the rest of the 85-99 NVM, is having the maximum high frequencies, which



| Table 10: The Normal modes (NVM) and the vibrational frequencies (ω_i) of Au_{35} at $\Delta E = 0$. | | | | | | |
|---|-------------------------------|------------|-------------------------------|------------|-------------------------------|--|
| NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | NVM (3N-6) | <i>ωi</i> [cm ⁻¹] | |
| 1 | 2.04 | 34 | 48.34 | 67 | 136.14 | |
| 2 | 3.09 | 35 | 49.18 | 68 | 138.71 | |
| 3 | 3.44 | 36 | 50.78 | 69 | 142.55 | |
| 4 | 6.06 | 37 | 53.20 | 70 | 145.31 | |
| 5 | 9.01 | 38 | 53.49 | 71 | 150.28 | |
| 6 | 9.69 | 39 | 57.39 | 72 | 152.88 | |
| 7 | 10.08 | 40 | 58.29 | 73 | 160.06 | |
| 8 | 11.56 | 41 | 61.94 | 74 | 163.33 | |
| 9 | 12.42 | 42 | 65.08 | 75 | 172.18 | |
| 10 | 13.40 | 43 | 65.43 | 76 | 173.57 | |
| 11 | 14.85 | 44 | 67.21 | 77 | 177.20 | |
| 12 | 15.57 | 45 | 69.64 | 78 | 179.07 | |
| 13 | 16.93 | 46 | 71.72 | 79 | 182.17 | |
| 14 | 17.86 | 47 | 73.88 | 80 | 185.42 | |
| 15 | 19.05 | 48 | 76.07 | 81 | 187.81 | |
| 16 | 19.83 | 49 | 76.67 | 82 | 191.55 | |
| 17 | 20.97 | 50 | 80.58 | 83 | 193.52 | |
| 18 | 22.30 | 51 | 81.64 | 84 | 196.65 | |
| 19 | 23.86 | 52 | 85.57 | 85 | 201.36 | |
| 20 | 24.22 | 53 | 87.49 | 86 | 204.70 | |
| 21 | 25.29 | 54 | 90.82 | 87 | 206.87 | |
| 22 | 28.19 | 55 | 92.64 | 88 | 211.61 | |
| 23 | 29.46 | 56 | 95.39 | 89 | 218.80 | |
| 24 | 30.74 | 57 | 98.79 | 90 | 224.10 | |
| 25 | 32.01 | 58 | 102.10 | 91 | 229.28 | |
| 26 | 35.10 | 59 | 103.18 | 92 | 237.01 | |
| 27 | 36.14 | 60 | 107.72 | 93 | 239.16 | |
| 28 | 37.75 | 61 | 111.41 | 94 | 243.05 | |
| 29 | 40.18 | 62 | 116.18 | 95 | 249.56 | |
| 30 | 43.03 | 63 | 120.32 | 96 | 254.40 | |
| 31 | 44.19 | 64 | 121.08 | 97 | 255.10 | |
| 32 | 45.49 | 65 | 128.81 | 98 | 261.72 | |
| 33 | 46.66 | 66 | 132 75 | 99 | 300.43 | |



geometrical structure of the Au_{35} cluster. Standard orientation of crystal shape at $\Delta E = 0$.

are $((\omega_i) - 201.36 - 300.43 \text{ cm}^{-1})$ falling within the range of Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹.

The double state degeneracy, ω_i : [{3.09, 3.44}; {9.01, 9.69}; {19.05, 19.83}; {53.20, 53.49}; {65.08, 65.43} and {76.07, 76.67}] in cm⁻¹. The degree of degeneracy has occurred below, as well as within the range of Far Infrared FIR, IR-C 200 - 10 cm⁻¹. Surely, such kind of spectrum could be highly possible to observe in the experimental calculations, except the first pair can be in silent modes. In addition to that due to the degree of degeneracy [which is being composed by] that gives a deep interpretation about the elliptical motion but that could be a single motion.

The results of DFT calculations by Gu, *et al.* [36] on Au_n Clusters with $32 \le N \le 35$ point to the existence of cage-like structures. Fa, *et al.* [29] suggested that the possible occurrences of the structures related to either fragments of the crystal or tubelike structures. These tube-like Au_n with larger surface area and hollow inner space may be important for fundamental chemistry research and in the future, have a wide range of applications in catalysis, biology, nanotechnology, etc.

The overall shape of the clusters: A spherical shape, a lenslike shape, and a cigar-like shape.

Can we observe the structural evolution and growth pattern of mid-sized gold atomic clusters?

From Figures 1-10 (that includes, (Figure 8a and Figure 8b)), a cluster growth path was identified from Au_{27} to Au_{35} : from Au_{27} to Au_{30} the clusters, which all have a single-atom core, grow by expanding the shell ($Au(@Au_m, m = 26-29)$; $Au_{33}(Au_4(@Au_{29}))$ can be viewed as adding an Au atom to the core of $Au_{32}(Au_3(\partial_1Au_{29}))$ whereas $Au_{34}(Au_4(\partial_{A}u_{30}))$ can be viewed as adding an Au atom to the shell of Au_{33} ($Au_4(@Au_{29})$). The Au_{34} structure, featuring a tetrahedral core and a 30-atom shell, is observed to be more round and quite robust, and the Au_{35} cluster can be viewed as adding an Au atom onto the surface of Au_{34} : $[(Au_4@Au_{30}) + Au]$. The observed core-shell growth path is interesting and may provide a valuable guide to the search for structures of larger gold atomic clusters. It is very excellent agreement with Nan Shao, et al. predictions [28], but their calculation was for the anionic clusters. Nonetheless, there may be some minor discrepancy that may be due to the minimum energy difference between the anionic and neutral clusters (which are more stable).

In Table A, the second column shows that the spectrum ranges vary with respect to the size of the clusters, the shape of the structures, and the arrangement of the atoms (inner core, and the overall outer surface of the edges), as well as the short and the long-range interactions due to the inter-nuclear attraction and the repulsive energies. We have designed a mini formula for the occupancy of the double (D) and the Triple (T) state degeneracy. Interestingly, the double state degeneracy occurred that is influenced by the nearest neighboring atoms, nuclei mass, as well as bond, strength, and their interactions, as well as the zig-zag circumstances of the outermost surface surrounded by

| Table A: The double and the triple state degree of degeneracy of the clusters, $Au_{26.35}$ at $\Delta E = 0$. | | | | | | | | | |
|--|-------------------------------|---|--|-----------------------------|--|--|--|--|--|
| Gold Nanoclusters (AuNCs) | Point Groups (PG) Symmetry | Spectral Range (Min - to - Max) <i>wi</i> [cm ⁻¹] | Double (D) & Triple (T) State Degeneracy [DT] ^(pairs) | Total Number of Pairs | Total Random Number (RN) of Different States of Equal Energy RN = (D*pairs + T*pairs) | Predicted Spectral Range Only for D, T- Degeneracies. A: Far Infrared FIR, IR - C 200 - 10 cm ⁻¹ B: Mid Infrared MIR, IR - C 3330 - 200 cm ⁻¹ X: Lesser than both, A and B | | | |
| Au26 | C_1 | 6.58 - 319.61 | $D^1 T^0$ | 1 | 2 | А | | | |
| Au27 | C_1 | 9.44 - 314.57 | $D^5 T^0$ | 5 | 10 | А | | | |
| Au28 | C_1 | 3.44 - 347.32 | $D^5 T^0$ | 5 | 10 | А | | | |
| Au29 | C_1 | 2.34 - 315.87 | D ³ T ⁰ | 3 | 6 | А | | | |
| Au ₃₀ | C_1 | 2.35 - 308.09 | D4 T0 | 4 | 8 | А | | | |
| <i>Au</i> ₃₁ | C_1 | 8.98 - 322.69 | D6 T0 | 6 | 12 | А | | | |
| Au32 | C_1 | 2.43 - 341.62 | $D^4 T^0$ | 4 | 8 | А | | | |
| Au33 | D_2 | 5.49 - 284.91 | D ¹⁴ T ⁰ | 14 | 28 | A, B, X | | | |
| Au ₃₄ | C_1 | 5.06 - 322.42 | D ⁶ T ⁰ | 6 | 12 | А | | | |
| Au ₃₅ | C_1 | 2.04 - 300.43 | D6 T0 | 6 | 12 | Α, Χ | | | |

them. Surely, we are able to see, the maximum total number of pairs that have occurred on the Au_{33} cluster among other clusters.

General information and its future application of our results

Above all, double-helical gold clusters, researchers can make use of these clusters for the electronic shell-closing ligandprotected gold cluster, because our cluster binds to a central atom to form a coordination complex. Valence states of the triangular and tetrahedral elementary blocks. Both elementary blocks triangular Au_3 and tetrahedral Au_4 entail only two valence electrons $[Au_3(2e) \text{ and } Au_4(2e)]$, thereby both having strong electron shell closures. Wen Wu Xu, *et al.* clearly shown in their Figures, the two valence electrons were delocalized in the shell-closing elementary blocks [84].

Gold clusters assemble into double-helical super crystals using similar pairing principles to those found between DNA base pairs, scientists have discovered. DNA has previously been used to create helical DNA-nanoparticle hybrid structures, but this was the first time nanoclusters have been known to self-assemble into a double helix. Without help from biological molecules, helices are difficult to build as they require a delicate balance between repulsive and attractive forces - in DNA, these are ionic interactions, and π stacking and hydrogen bonding, respectively [85].

Liganded gold clusters have attracted intensive interest over the past 15 years owing to their broad and practical applications in catalysis [86], electrochemistry [87], quantum electronics [88] and biomedicine [89 - 92]. A grand challenge to scientists in this field, however, is the precise determination of atomic structures of liganded gold clusters.

Our findings results will definitely help to choose any right suitable candidates (metals or biological molecules) for doping and that will be useful for the future healing of human health diseases and industrial applications.

Conclusion

We are first to present, the vibrational frequencies of

medium-sized gold clusters (Au26-35) and the shell-like structure (of course, they are part of the family of so-called full-shell clusters) by using the numerical finite-differentiation method along with the DFTB approach. The DFTB-based calculations work is accomplished to study the gold cluster that is variable with the different sizes. We have observed the vibrational spectrum with excellent accuracy, the starting and the end ranges vary between 2.04 and 347.32 cm-1 at $\Delta E = 0$. Moreover, amazingly the occupancy of the multiple double degeneracies is revealed in all the clusters (refer to Table A). We have compared some of our results, which have an excellent agreement, with the less or availability of the experimental and the theoretical predictions.

In addition to that, we have observed the vibrational properties of the gold clusters in order to explore the stability and the structures. IR spectroscopy is considered the harmonic motion of atoms. Vibrational frequency in the covalent bonding and every covalent bond represents the different specific frequency that vibrates with several modes like scissoring, rocking, and stretching. Above all, we have pinpointed the correct location of the spectrum, through Far Infrared FIR, IR-C 200 - 10 cm⁻¹, and Mid Infrared MIR, IR-C 3330 - 200 cm⁻¹. Our prediction will help the researchers to develop a range of potential applications such as catalysis, biomedicine, imaging, optics, and energy conversion. In conclusion, our present calculations of the frequency spectrum are the predictions to be confirmed when the experimental data become available, also, it is expected that this work will be beneficial for the modification of the characteristics of the gold clusters, and further will cause the major development in technological and scientific in the future.

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